

Model Answer

جامعة الفيوم
كلية الهندسة

العام الدراسي : ٢٠١٩ / ٢٠٢٠

الفصل الدراسي : الأول

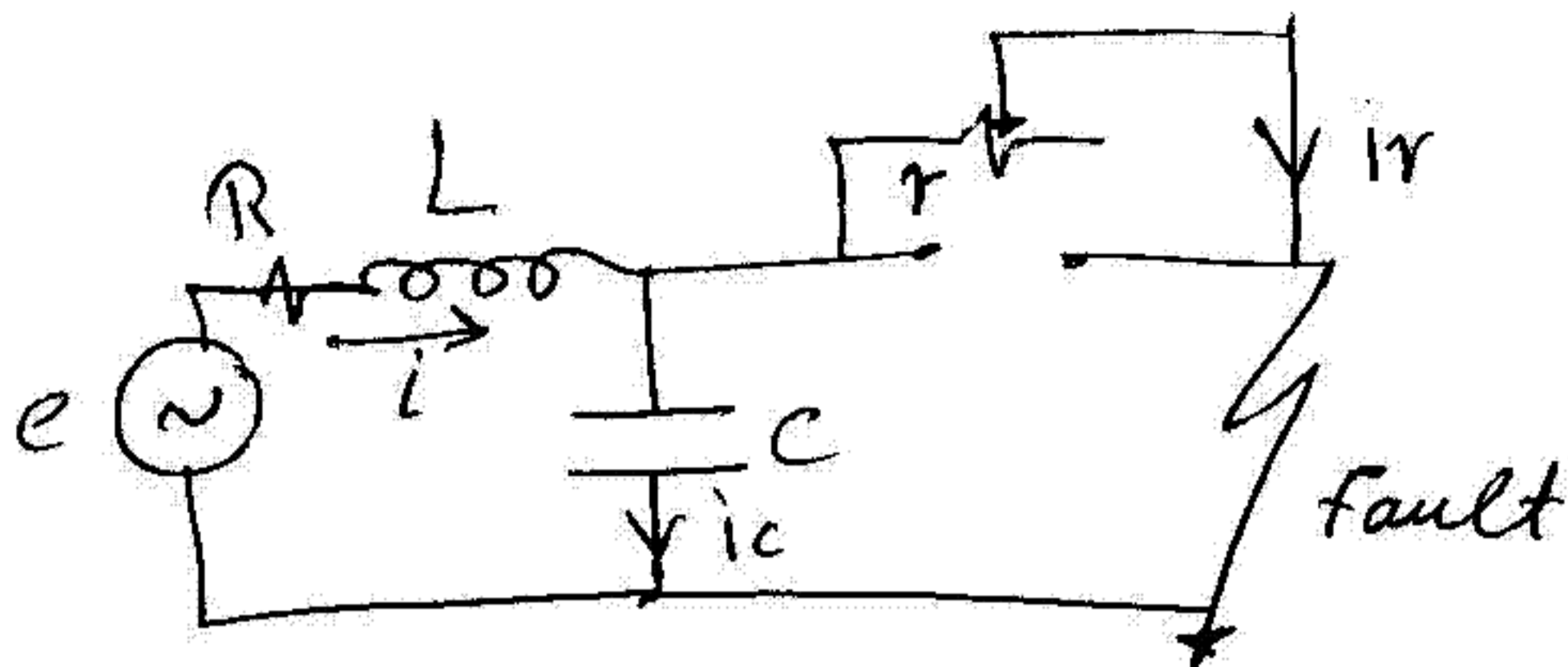
قسم الهندسة الكهربائية - شعبة الآلات والعلوم الكهربائية

المرحلة الرابعة

مادة : أجهزة الوقاية والحماية

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Q1
a)



$$e = iR + L \frac{di}{dt} + \frac{1}{C} \int ic dt$$

but $\frac{1}{C} \int ic dt = ir$ $\therefore \frac{1}{C} = r \frac{dir}{dt}$

$$\therefore ic = rC \frac{dir}{dt} \quad \& \quad i = ir + ic$$

$$\therefore 0 = \left[ir + rC \frac{dir}{dt} \right] R + L \frac{dir}{dt} + L rC \frac{d^2 ir}{dt^2} + ir r$$

[homogeneous solution]

$$\therefore \frac{d^2 ir}{dt^2} + \underbrace{\frac{rCR + L}{LrC}}_{B_1} \frac{dir}{dt} + \underbrace{\frac{R+r}{LrC}}_{B_2} ir = 0$$

$$\therefore \frac{d^2 ir}{dt^2} + B_1 \frac{dir}{dt} + B_2 ir = 0$$

The roots of the equation are given as follows

-2-

$$\frac{-B_1 \pm \sqrt{B_1^2 - 4B_2}}{2}$$

for oscillations to take place \rightarrow complex roots

$$\therefore \omega = \sqrt{-\left(\frac{R^2}{L^2} + \frac{2R}{LrC} + \frac{1}{r^2C^2} - \frac{4}{LC} - \frac{4R}{rLC}\right)}$$

$$= \sqrt{-\frac{R^2}{4L^2} + \frac{R}{2LrC} - \frac{1}{4r^2C^2} + \frac{1}{LC}}$$

$$= \sqrt{\frac{1}{LC} - \left(\frac{R^2}{4L^2} - \frac{R}{2LrC} + \frac{1}{4r^2C^2}\right)}$$

$$= \sqrt{\frac{1}{LC} - \left(\frac{R}{2L} - \frac{1}{2rC}\right)^2}$$

$$\therefore f = \frac{1}{2\pi} \omega \rightarrow \textcircled{1}$$

$$L = 0.15 \text{ H}; R = 12 \Omega; C = 0.15 \mu\text{F}; r = 1000 \Omega$$

$$\text{Sub in } \textcircled{1} \therefore f = 922.5277 \text{ Hz}$$

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For critical damping $B_1^2 - 4B_2 = 0$

$$\left(\frac{rCR + L}{Lrc} \right)^2 - 4 \left(\frac{R+r}{Lvc} \right) = 0$$

$$\frac{(rCR + L)^2}{Lrc} - 4(R+r) = 0$$

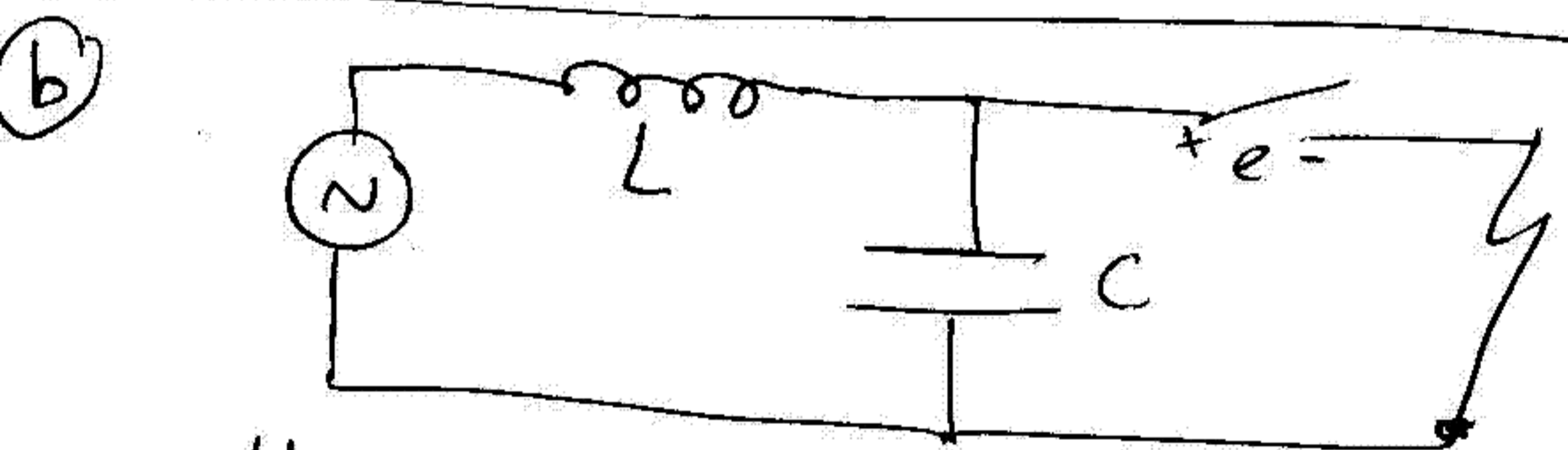
$$(rCR + L)^2 - 4Lrc(R+r) = 0$$

$$r^2 c^2 R^2 + 2rCL + L^2 - 4LrRC - 4Lr^2 c = 0$$

$$r^2(c^2 R^2 - 4Lc) + r(2CL - 4LRC) + L^2 = 0$$

Sub with the values of L, c, and R

$$\therefore r = 497.0179 \Omega$$



$$\text{Maximum RRRV} = \frac{E_m}{\sqrt{LC}} = \frac{13 \times 10^3 \times \sqrt{2}}{\sqrt{3} \times \sqrt{LC}}$$

where $L = 0.014 \text{ H}$ & $C = 0.012 \mu\text{F}$

$$\therefore \text{Max RRRV} = 818.923 \text{ MV/s}$$

(4)

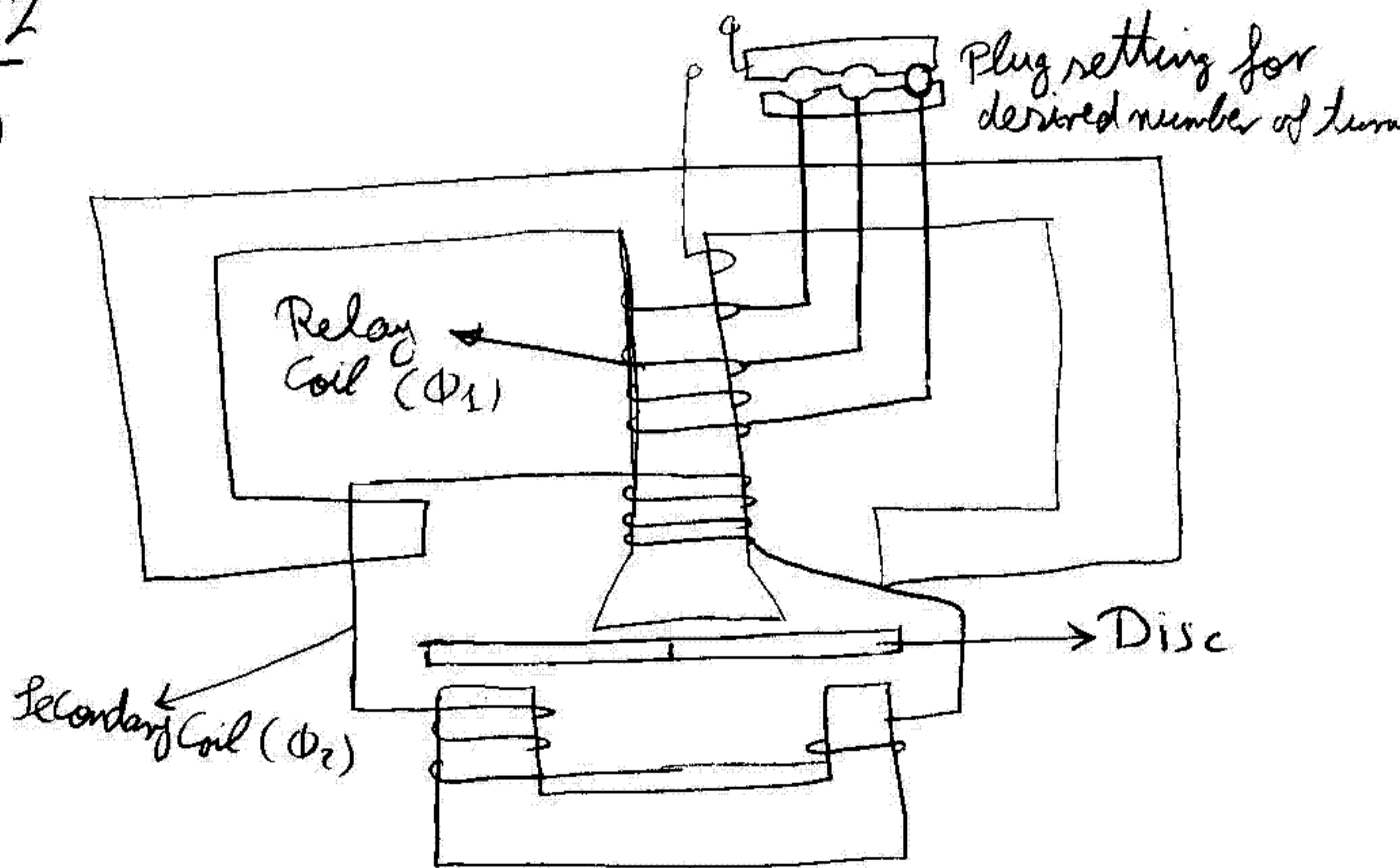
$$e_{\max} = 2E_m = 21.2289 \text{ KV}$$

$$f = \frac{1}{2\pi\sqrt{LC}} = 12.279 \text{ KHz}$$

$$\frac{t}{\sqrt{LC}} = \frac{\pi}{2} \therefore t = 20.3598 \mu\text{s}$$

Q2

(a)



Torque is produced on the disc by the interaction between flux and eddy current. The relay coil is tapped at several points, to select the desired plug setting through a knob.

The phase angle between the 2 fluxes Φ_1 & Φ_2

[5]

is adjusted by a reactance connected in parallel to the secondary coil.

$$\text{Net force } F = (F_2 - F_1)$$

$$(F_2 - F_1) \propto (\Phi_2 i \Phi_1) - (\Phi_1 i \Phi_2)$$

$$i \Phi_1 = \frac{d\Phi_1}{dt} \propto \Phi_1 \cos \omega t$$

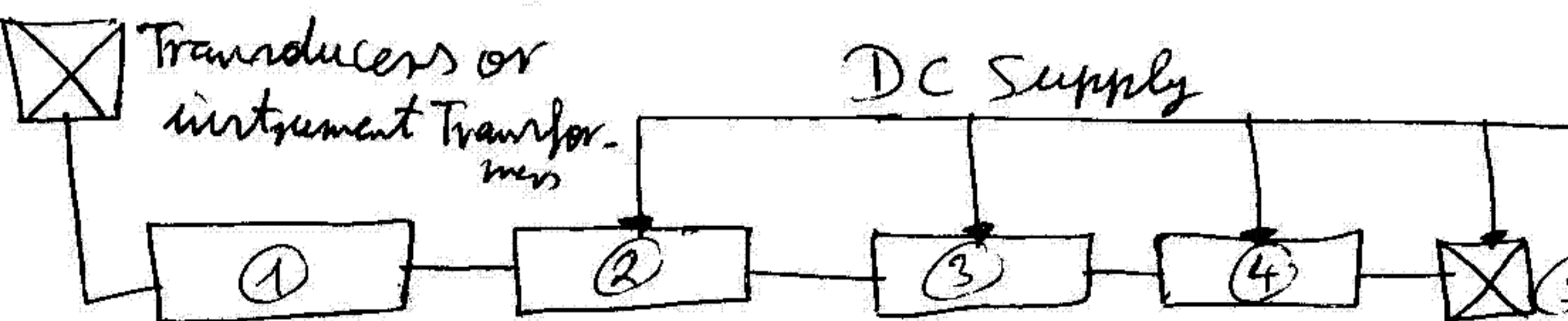
$$i \Phi_2 = \frac{d\Phi_2}{dt} \propto \Phi_2 \cos(\omega t + \theta)$$

$$\therefore F \propto \Phi_2 \sin(\omega t + \theta) \Phi_1 \cos \omega t - \Phi_1 \sin \omega t \Phi_2 \cos(\omega t + \theta)$$

$$\therefore F \propto \Phi_1 \Phi_2 [\sin(\omega t + \theta) \cos \omega t - \sin \omega t \cos(\omega t + \theta)]$$

$$\therefore F \propto \Phi_1 \Phi_2 \sin \theta$$

(b) Static Relay



Simplified block diagram of a Static Relay

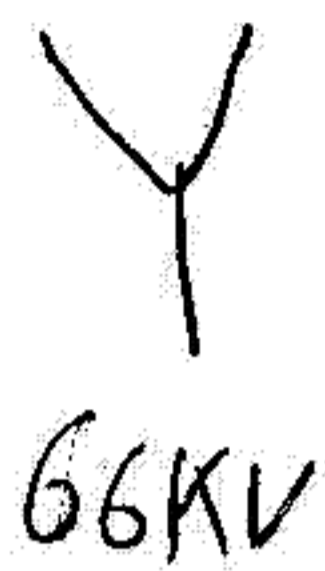
(6)

- ① Rectifier Circuit to convert from AC to DC
- ② Relay-Measuring circuit consisting of comparator, level detector, filter and voltage stabilizer.
- ③ Amplifier to magnify the signal.
- ④ Output device to energize the trip coil.
- ⑤ Trip Circuit.

Static relays can be arranged to respond to electric inputs. The other forms of inputs, such as heat, light, magnetic field, travelling waves etc can be suitably converted into equivalent analogue or digital signals and then fed to the Static Relay.

$\frac{\phi}{3}$
a)

(7)



$$I_{L\Delta} = 400A$$

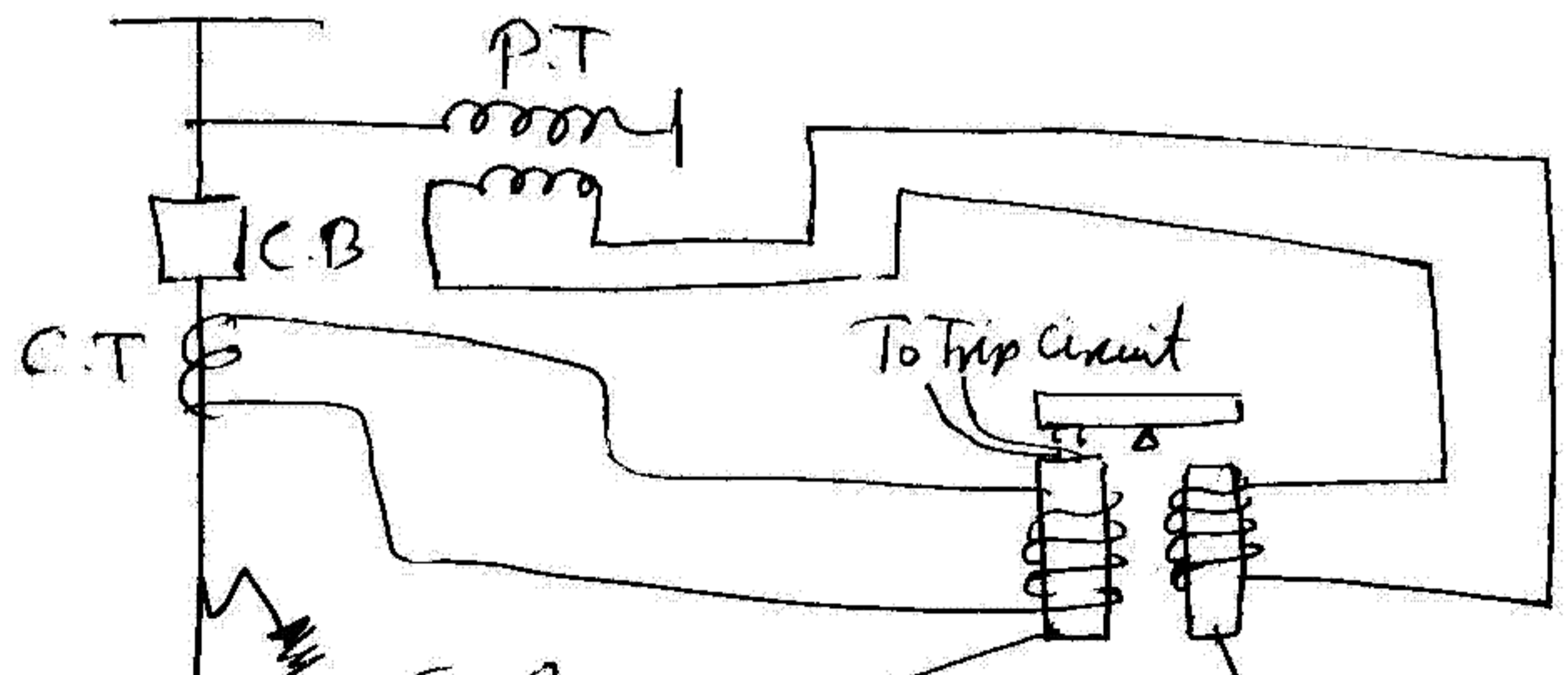
$$I_{LY} = \frac{11 \times 400}{66} = 66.67A$$

$$I_{LC.T} = 5A$$

∴ Primary side turns ratio = $66.67 : \frac{5}{\sqrt{3}}$

$$\approx 115 : 5$$

(b) Plain impedance Distance Relay



Coil actuated by current

Current actuated by Volts

(8)

T_1 = operating Torque ; T_2 = restraining Torque ; T_3 = Spring Torque

I = Current proportional to feeder Current.

V = Voltage \propto to feeder Voltage

K_3 = Spring Constant

$$T = \underbrace{K_1 I^2}_{T_1} - \underbrace{K_2 V^2}_{T_2} - \underbrace{K_3}_{T_3}$$

The relay is on the verge of operation if $T=0$

$$\therefore K_2 V^2 = K_1 I^2 - K_3$$

$$\frac{V^2}{I^2} = \frac{K_1}{K_2} - \frac{K_3}{K_2 I^2}$$

but $\frac{V}{I} = Z$

$$\therefore Z^2 = \frac{K_1}{K_2} - \frac{K_3}{K_2 I^2}$$

$$\therefore Z = \sqrt{\frac{K_1}{K_2} - \frac{K_3}{K_2 I^2}}$$

but $\frac{K_3}{K_2 I^2} \ll \frac{K_1}{K_2}$

$$\therefore Z = \sqrt{\frac{K_1}{K_2}} = \text{Constant}$$

(+a) The initial inrush magnetizing current has a high component of 2nd harmonic.

order of harmonic	amplitude as % of fundamental
2 nd	63
3 rd	23
4 th	5
5 th	4
6 th	3
7 th	2

The main protection against the magnetizing inrush current is the second harmonic restraint. It contains a 100 Hz blocking filter in operating coil and 50 Hz blocking filter in restraining coil. During inrush currents the 2nd harmonic component is predominant and the operating relay is blocked.

During short circuits, 50 Hz component is predominant, hence operating relay operates and relay contact circuit is closed.

(11)

b) $I_f = 2000A$

for relay 1 $I_R = 10A$

$$\therefore P.S.M = \frac{2000}{200 \times 1} = 10$$

from C.I.C's O.T = 3s

but actual O.T = $3 \times 0.2 = 0.6s$

$$\therefore O.T \text{ for second Relay} = 0.6 + 0.5 = 1.1s.$$

for the second Relay $P.S.M = \frac{2000}{200 \times 1.25} = 8$

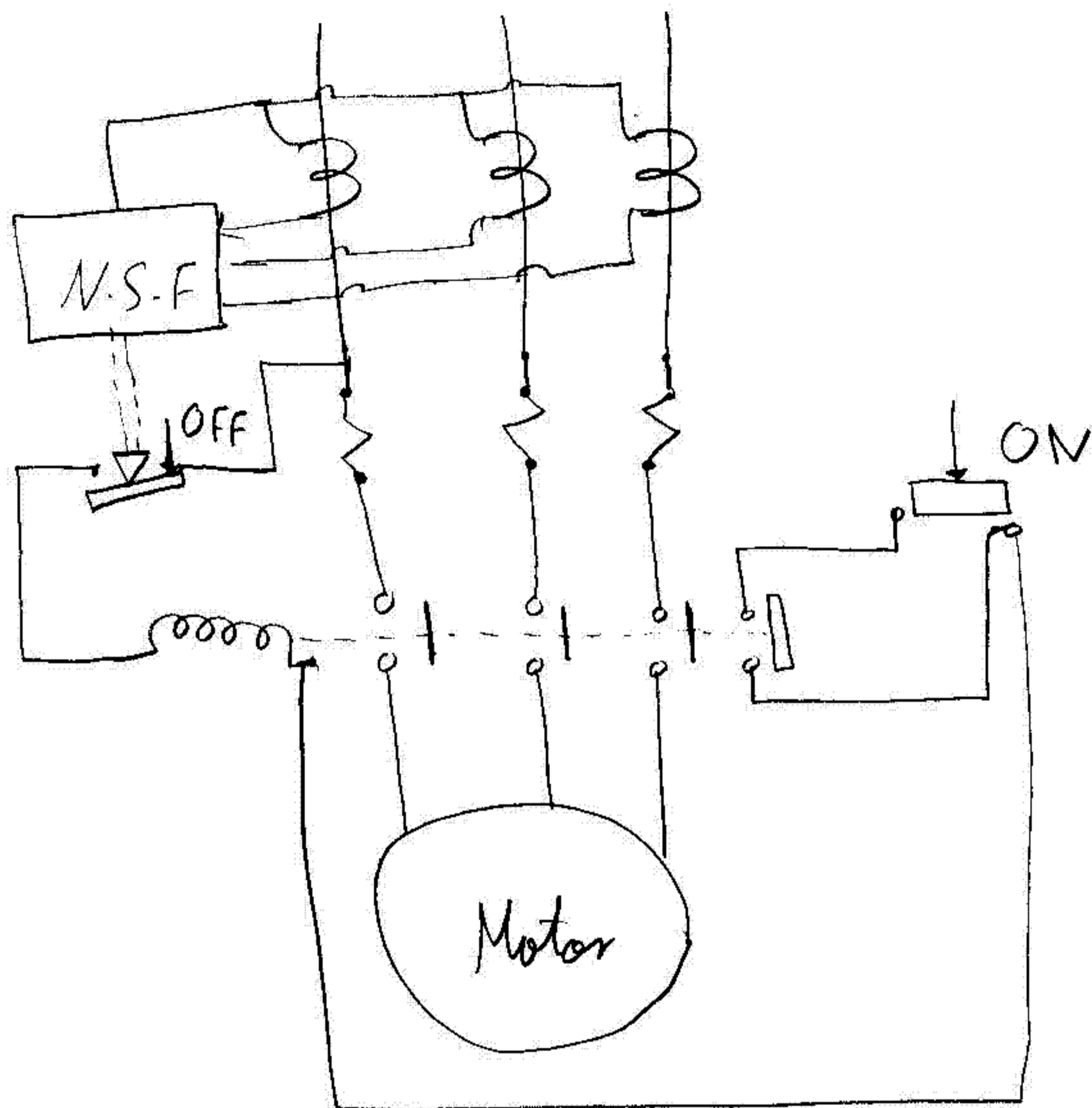
from C.I.C's O.T =

\therefore actual O.T = 1.1s

$\therefore P.S.M = \frac{\quad}{1.1}$

$$T.S.M = \frac{1.1}{\text{Time from C.I.C}} = \frac{1.1}{3.3} = 0.333$$

(a)



$NSF \equiv$ Negative Sequence Filter

The -ve seq. filter receives the 3 phase line currents. Its output is fed to a level detector, which sends tripping command to the starter or circuit breaker when the -ve sequence current exceeds a pre-set limit. It is so harmful, because the motor draws heavy current and harmonics are generated, which cause overheating to the motor.

(13)

(5b)

$$I_f = 0.8 \times \frac{2000}{5} = 320 \text{ A}$$

$$V_f = 320 \times 12 = 3840 \text{ V}$$

$$\therefore \% \text{ of unprotected winding} = \frac{3840}{\frac{11 \times 10^3 \times 1}{\sqrt{3}}} = 60.46\%$$

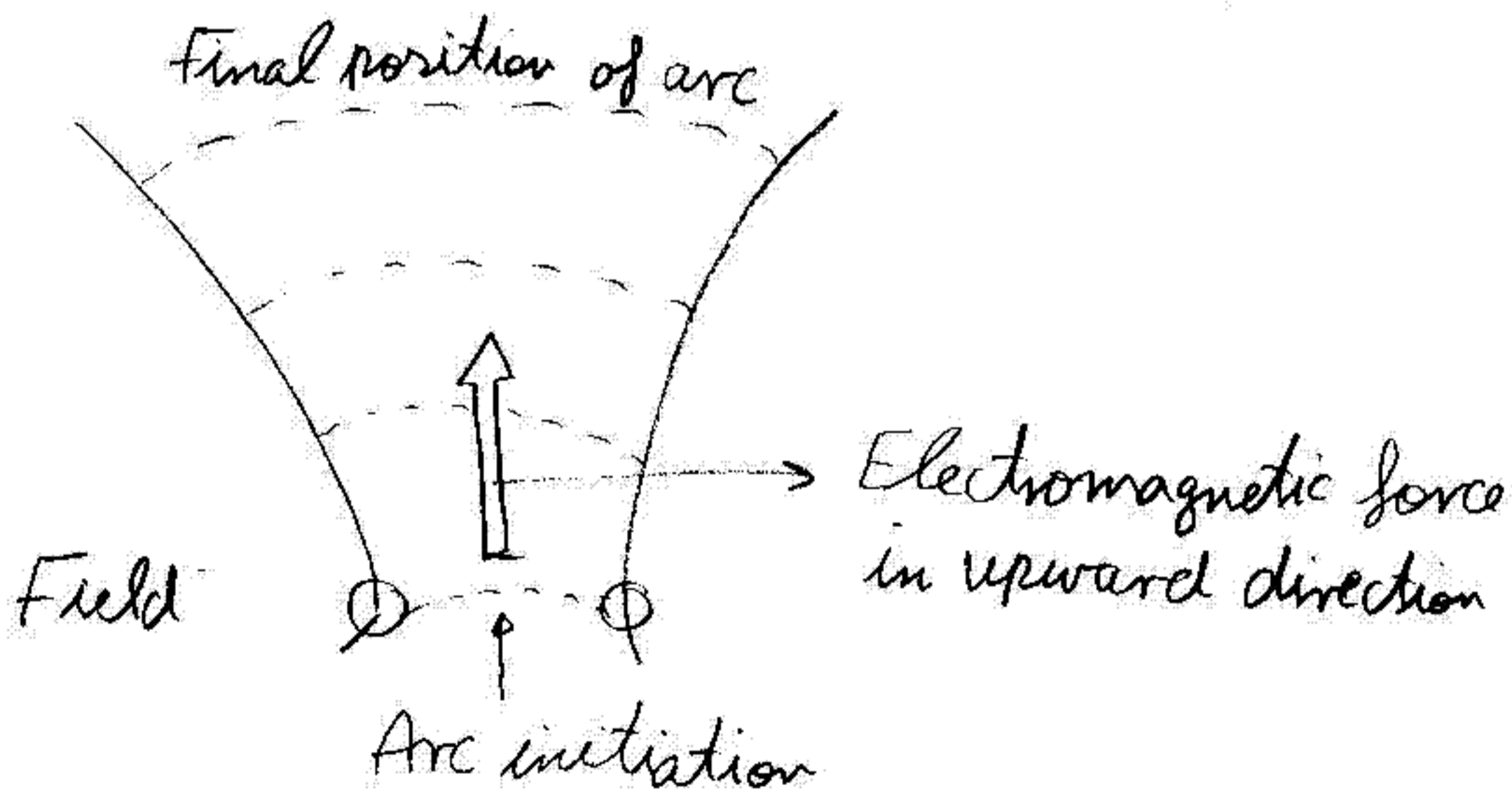
$$\therefore \% \text{ of protected winding} = 39.54\%$$

If 90% are protected \therefore 10% are unprotected

$$\therefore V_f = \frac{11 \times 10^3}{\sqrt{3}} \times 0.1 = 635.085 \text{ V}$$

$$R_f = \frac{V_f}{I_f} = 1.985 \Omega$$

(c)



In this method the arc length is increased by using arc runners which are horn like blades of conductors.

material. The arc runners are connected to arcing contacts and it is in the shape of letter 'V'. The arc is initiated at the bottom and blows upwards due to electromagnetic force. Due to this arc length increases and consequently arc is extinguished.

(d) An auxiliary compressed air system is required. This supply air to air reservoir of the breaker. During the opening operation, the air is allowed to enter the extinction chamber which pushes away moving contacts. The contacts are separated and the blast of air will take ionized gases with it and helps in extinguishing the arc. There are two major types, cross blast and axial blast.