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Solution of Foundation Design Exam (2010)

(Q1)

$$R = 120 + 80 = 200 \text{ t}$$

$$l_1 = \frac{80 \times 3.10}{200} = 1.24 \text{ m} \quad ; \quad l_2 = 3.10 - 1.24 = 1.86$$

$$\frac{A}{2} = X + C_2 + \frac{a_2}{2} + l_2 = 0.30 + 0.50 + 0.3 + 1.86 = 2.96 \text{ m}$$

$$A = 5.92 \approx 5.95 \text{ m}$$

$$C_1 = \frac{5.95}{2} - 0.30 - 0.4 - 1.24 = 1.035 \text{ m}$$

$$B = \frac{1.15 \times 200}{15 \times 5.95} = 2.57 = 2.60 \text{ m}$$

Plain concrete dim. $5.95 \times 2.60 \times 0.30$

$$A_1 = 5.95 - 0.60 = 5.35 \text{ m}$$

$$B_1 = 2.60 - 0.60 = 2.00 \text{ m}$$

$$P_m = \frac{200 \times 1.50}{5.35 \times 2.00} = 28.0 \text{ t/m}^2 \quad w = 56.07 \text{ t/m}$$

* Bending moment;

$$M_2 = 56.07 (0.515)^2 / 2 = 7.44 \text{ m.t}$$

$$M_1 = 56.07 (1.035)^2 / 2 = 30.03 \text{ m.t}$$

M_{\max} at zero shear

$$56.07 * z - 120 * 1.50 = 0.0 \quad z = 3.21 \text{ m}$$

$$M_{max} = 56.07 (3.21)^2 / 2 - 120 \times 1.50 (3.21 - 1.435) = 30.65 \text{ m.t}$$

$$d = 5 \sqrt{\frac{30.65 \times 10^5}{250 \times 200}} = 39.15 \text{ cm} \quad t = 45 \text{ cm}$$

(1) check of shear:

$$Q_s = 120 \times 1.50 - (1.035 + 0.80 + 0.5) \times 56.07 = 49.08 \text{ t}$$

$$q_s = \frac{49.08 \times 10^3}{200 \times 40} = 6.13 < 9.81 \quad \text{safe.}$$

(2) check of punching:

$$Q_p = 120 \times 1.50 - 28.0 (0.80 + 0.40) (0.40 + 0.40) = 153.12 \text{ t}$$

$$A_p = 2 [(0.8 + 0.40) + (0.40 + 0.40)] = 4.0$$

$$q_p = \frac{153.12 \times 10^3}{4.0 \times 10^4} = 3.828 \text{ kg/cm}^2 < 12.9 \quad \text{o.k.}$$

(3) Design of Hidden Beams

$$\text{Beam H.B}_1 \quad w_1 = \frac{1.50 \times 120}{2.00} = 90 \text{ t/m}$$

$$M = 90 \times (2.0 - 0.4)^2 / 8 = 28.80 \text{ m.t}$$

$$d = 5 \sqrt{\frac{28.80 \times 10^5}{120 \times 250}} = 48.98 > d \quad \therefore \text{take } d = 50 \text{ cm}$$

Beam H.B2 $w_2 = \frac{80 \times 1.50}{2} = 60 \text{ t/m}^1$

$M = 60 \times (2 - 0.4)^2 / 8 = 19.2 \text{ m.t}$

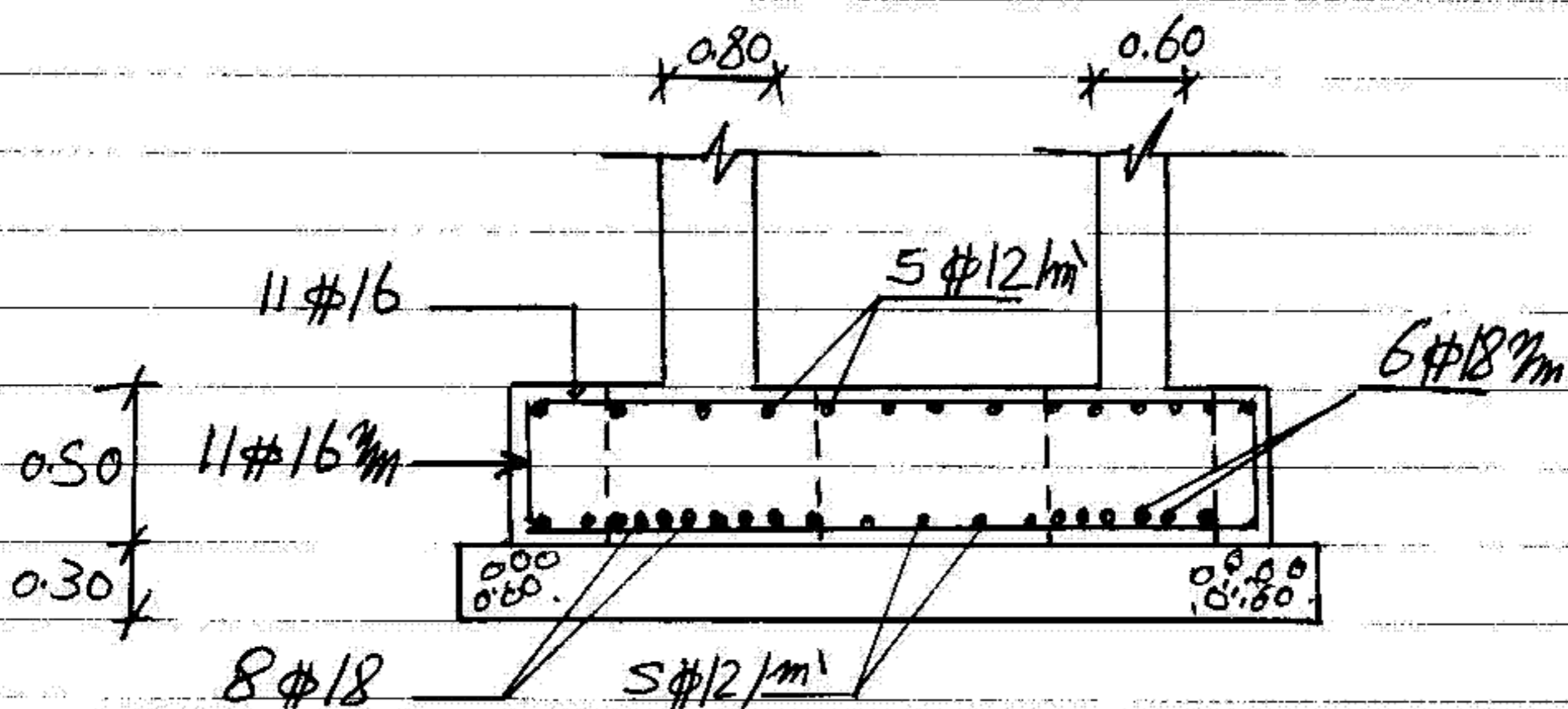
$d = 5 \sqrt{\frac{19.2 \times 10^5}{100 \times 250}} = 43.8 < 50 \text{ cm o.k}$

$A_s(\text{top}) = \frac{30.65 \times 10^5}{3600 \times 50 \times 0.826} = 20.6 \text{ cm}^2 \quad 11 \#16 \text{ mm}$

$A_s(\text{bot}) = \frac{30.03 \times 10^5}{3600 \times 50 \times 0.826} = 20.19 \text{ cm}^2 \quad 11 \#16 \text{ mm}$

$A_s(\text{H.B1}) = \frac{28.8 \times 10^5}{3600 \times 50 \times 0.826} = 19.37 \quad 8 \#18 \text{ mm}$

$A_s(\text{H.B2}) = \frac{19.2 \times 10^5}{3600 \times 50 \times 0.826} = 12.91 \quad 6 \#18 \text{ mm}$



Q21

* External footing

$$3.5 * R_e = n * l_0 * (1.5 + 1.0 + 2.00 - 0.2) \quad \therefore R_e = 12.29 \text{ m} \pm$$

* Bearing capacity

$$\frac{12.29 \text{ m}}{2 * 2} = 2.5 \quad \therefore n = 8.14$$

* depth of footing and RFT

$$P_{me} = \frac{12.29 \text{ m} * 1.50}{2 * 2} = 4.61 \text{ m} \quad W_e = 9.22 \text{ m}$$

$$\therefore M_u = 4.61 * n * \left(\frac{2 - 0.6}{2}\right)^2 / 2 = 1.13 \text{ m}$$

$$5.5 = 5 \sqrt{\frac{1.13 \text{ m} * 10^5}{250 * 100}} \quad n = 26.7$$

$$6 * 2 = \frac{1.13 \text{ m} * 10^5}{5.5 * 3600 * 0.826} \quad n = 17.36$$

* check of shear

$$Q_s = 1.13 \text{ m} * \left(\frac{2 - 0.6 - 0.55}{2}\right) = 0.1695 \text{ m}$$

$$q_s = \frac{0.1695 \text{ m} * 10^3}{100 * 5.5} = 0.0308 \text{ m} = 9.68$$

$$\therefore n = 314$$

* Internal footing:-

$$R_i = 20m * 1.5 = 30m$$

* Bearing capacity

$$\frac{1.5 * 30m}{3 * 3} = 25 \quad m = 9.78 \approx 9.00$$

* Depth of footing and RFT

$$P_{m_i} = \frac{30m}{3 * 3} = 3.33m \quad w_i = 10m$$

$$M_u = 3.33m \left(\frac{3 - 0.6}{2} \right)^2 / 2 = 2.398m$$

$$55 = 5 \sqrt{\frac{2398m \times 10^5}{250 * 100}} \quad \therefore m = 12.6 \approx 12$$

$$12 = \frac{2.398m \times 10^5}{3600 * 55 * 0.826} \quad m = 8.18 = 8$$

* check of shear

$$Q_s = 3.33m \left(\frac{3 - 0.6}{2} - 0.55 \right) = 2.165m$$

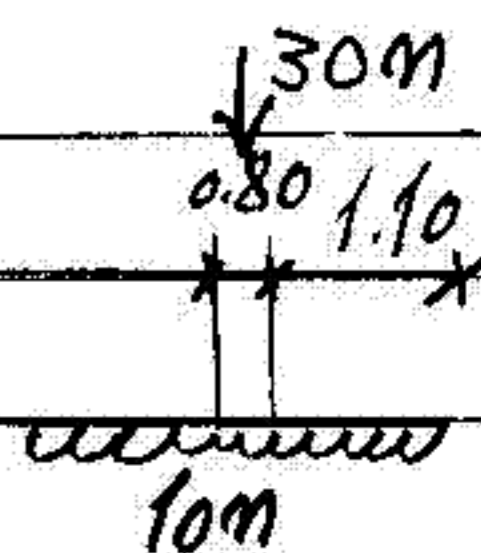
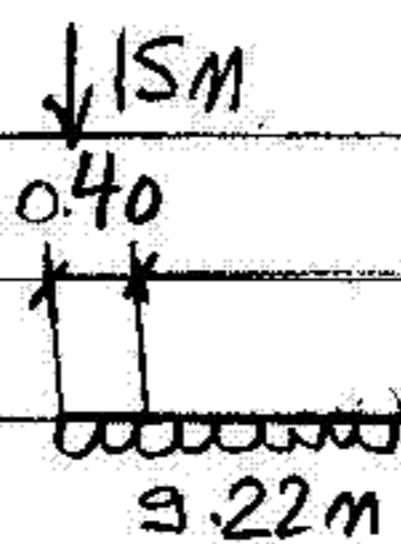
$$q_s = \frac{2.165 * m \times 10^3}{100 * 55} = 0.394m = 9.68 \quad m = 24.57 = 24$$

* Strap Beam



$$W_e = 9.22 \text{ m}$$

$$W_i = 10 \text{ m}$$



$$M_1 = 10 \text{ m} \times (1.10)^2 / 2 = 6.05 \text{ m}$$

M_{max} at zero shear

$$15 \text{ M} - z \times 9.22 \text{ m} = 0.0 \quad z = 1.63 \text{ m}$$

$$M_{max} = 15 \text{ M} (1.63 - 0.2) - 9.22 \text{ m} \times \frac{(1.63)^2}{2} = 9.20 \text{ M}$$

$$IIS = 5 \sqrt{\frac{9.20 \text{ M} \times 10^5}{250 \times 55}} \quad \therefore n = 7.9 \approx 7$$

$$\text{Top } 38 = \frac{9.20 \text{ M} \times 10^5}{3600 \times 115 \times 0.826} \quad n = 14.12 \approx 14$$

$$\text{bot } 30.4 = \frac{6.05 \text{ m} \times 10^5}{3600 \times 115 \times 0.826} \quad n = 17.18 \approx 17$$

* check of shear



$$Q_s = 30 \text{ m} - 10 \text{ m} (1.10 + 0.80 + 1.15) = 0.5 \text{ M}$$

$$q_s = \frac{0.5 \text{ M} \times 10^3}{115 \times 60} = 9.68 \quad n = 133.5$$

\therefore total no. of floors 8 floors
No. of extra floors = 4 floors.

(Q4):

* ultimate capacity of pile ($d = 45$) & ($L = 18\text{m}$)

$$P_u = P_{bu} + P_{su}$$

$$P_{bu} = c N_c \alpha_c A_p = 2.325 \times 10 \times 9.33 \times (0.45)^2 \times \frac{\pi}{4} = 34.5\text{t}$$

$$P_{su} = c_a \times \pi d \times L = 1.5375 \times 10 \times 0.5 \times \pi \times 0.45 \times 18 = 195.62\text{t}$$

$$P_u = 34.5 + 195.62 = 230.1\text{t}$$

* ultimate capacity of pile ($d = 60\text{cm}$) & ($L = 15\text{m}$)

$$P_{bu} = c N_c \alpha_c A_p = 2.0625 \times 10 \times 9.33 (0.6)^2 \times \frac{\pi}{4} = 54.4\text{t}$$

$$P_{su} = c_a \times \pi d \times L = 1.40625 \times 10 \times 0.5 \times \pi \times 0.60 \times 15 = 198.88\text{t}$$

$$P_u = 54.4 + 198.88 = 254.21$$

* The short pile with greater diameter has a higher ultimate capacity.

(Q3)

ultimate load pile capacity

$$P_u = P_{bu} + P_{su}$$

$$P_{bu} = q_p N_q \lambda_q A_p$$

$$q_p = \sum \gamma h = 2 \times 1.9 + 2 \times 1.8 + 10 \times 0.90 = 16.4 \text{ t/m}^2$$

$$P_{bu} = 120 \times 16.40 \times (0.25)^2 = 123 \text{ t}$$

$$P_{su} = e_{qv} \times (4b) L \times \tan \delta$$

$$e_{qv} = (2 \times 1.9 + 2 \times 1.8 + 3 \times 0.90) (1 - \sin 36)$$

$$e_{qv} = 4.16 \text{ t/m}^2$$

$$P_{su} = 4.16 \times 4 \times 0.25 \times 10 \times \tan 27 = 21.21 \text{ t}$$

(neglect friction fill layer)

$$P_u = 123 + 21.21 = 144.2 \text{ t}$$

$$P_{all} = 144.2 / 2.5 = 57.68 \text{ t}$$

$$P_{mat} = 500 \times 0.25 \times 0.25 = 31.25 \text{ t}$$

$$P_{safe} = 31.25 \text{ t}$$