

## **On Certain Classes of** *p***-Valent Meromorphic Functions** Associated with a Family of Integral Operators

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Abstract. This paper gives some inclusion relationships of certain class of p-valent meromorphic functions which are defined by using the linear operator  $Q_{a,\beta,\gamma}^{p,\mu}$ . Further, a property preserving integrals is considered.

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## 1. Introduction

For any integer m > -p, let  $\Sigma_{p,m}$  denote the class of all meromorphic functions f of the form:

$$f(z) = z^{-p} + \sum_{k=m}^{\infty} a_k z^k \quad (p \in \mathbb{N} = \{1, 2, \ldots\}),$$
(1)

which are analytic and *p*-valent in the punctured disc  $U^* = \{z \in \mathbb{C} : 0 < |z| < 1\} = U \setminus \{0\}$ . For convenience, we write  $\Sigma_{p,-p+1} = \Sigma_p$ . If f and g are analytic in U, we say that f is subordinate to g, written symbolically as,  $f \prec g$  or  $f(z) \prec g(z)$ , if there exists a Schwarz function w, which (by definition) is analytic in U with w(0) = 0 and |w(z)| < 1 ( $z \in U$ ) such that f(z) = g(w(z)) ( $z \in U$ ). In particular, if the function g is univalent in U, we have the equivalence [see for example 5]:

$$f(z) \prec g(z) \Leftrightarrow f(0) = g(0) \text{ and } f(U) \subset g(U).$$

For functions  $f \in \Sigma_{p,m}$  given by (1), and  $g \in \Sigma_{p,m}$  defined by

$$g(z) = z^{-p} + \sum_{k=m}^{\infty} b_k z^k \quad (m > -p; p \in \mathbb{N}),$$
(2)

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85

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