

Fayoum University	Structural Analysis & Mechanics III	Third Civil Year 2015-2016
Department of Civil Engineering	2 nd Term - Mid-Term Exam	Time: 105 min.
Name (باللغة العربية) :	Sec (...) N (...)	رقم الجلوس (.....)

Please solve in sequence similar to that adopted in lecturers and illustrate the DOF and connectivity on the structure.

Q1. Use Matrix Displacement Method (Assembly Approach) to draw B.M.D., S.F.D. and N.F.D. for the illustrated structure. Also, find the force in the spring. Consider the axial deformation for member BC.

Problem			$E=2100 \text{ t/cm}^2$ Area of link $AB=10 \text{ cm}^2$ Area of beam $BC=100 \text{ cm}^2$ Inertia of beam $BC=20833.333 \text{ cm}^4$ Spring stiffness $K_s=7 \text{ t/cm}$	D.O.F & connectivity														
	Find P	$P = \left\{ \begin{matrix} \\ \\ \\ \end{matrix} \right\}$			Member AB Element Stiffness Matrix in Local Coordinates $\tilde{K} = \left[\begin{matrix} \\ \\ \end{matrix} \right]$													
Member AB	Transformation Matrix	$T = \left[\begin{matrix} \\ \\ \end{matrix} \right]$		Element Stiffness Matrix in Global Coordinates $K = \left[\begin{matrix} \\ \\ \end{matrix} \right]$														
Member BC	Transformation Matrix	$T = \left[\begin{matrix} \\ \\ \end{matrix} \right]$		Element Stiffness Matrix in Global Coordinates $K = \left[\begin{matrix} \\ \\ \end{matrix} \right]$														
V-C Table	Truss <table border="1"> <thead> <tr> <th>Member</th> <th>end P</th> <th>end q</th> </tr> </thead> <tbody> <tr> <td>1</td> <td></td> <td></td> </tr> </tbody> </table>			Member	end P	end q	1			Frame <table border="1"> <thead> <tr> <th>Member</th> <th>end P</th> <th>end q</th> </tr> </thead> <tbody> <tr> <td>2</td> <td></td> <td></td> </tr> </tbody> </table>			Member	end P	end q	2		
	Member	end P	end q															
1																		
Member	end P	end q																
2																		
Structure Stiffness Matrix	Symbolic	$K = \left[\begin{matrix} \\ \\ \\ \end{matrix} \right]$																
	Numbers	$K = \left[\begin{matrix} \\ \\ \\ \end{matrix} \right]$																

<i>Solution of Equations</i>	$U = K^{-1}P = \left\{ \begin{array}{l} \\ \\ \end{array} \right\}$	<i>Force in member AB</i>	$U = \left\{ \begin{array}{l} \\ \\ \end{array} \right\}$	$\tilde{U} = \left\{ \begin{array}{l} \\ \\ \end{array} \right\}$	$\tilde{P} = \left\{ \begin{array}{l} \\ \\ \end{array} \right\}$	Choose Tension Compression			
<i>Force in member BC</i>	$\tilde{U} = \left\{ \begin{array}{l} \\ \\ \end{array} \right\}$	$\tilde{P} = \left\{ \begin{array}{l} \\ \\ \end{array} \right\}$	<i>M, N & Q Diagrams</i>	B.M.D.		S.F.D.		N.F.D.	

Q2. Use the reduction theory to find the deflection at C. Use statically determinate system to draw B.M.D. of applied loads and use statically indeterminate system to draw B.M.D. due to unit downward load at C.

Problem			Moment due to applied loads	determinate system
Moment due to unit load	indeterminate system	M₁ diagram	Moment due to unit load	determinate system
M₁ diagram	M₀ diagram	$\delta_c =$	$\delta_c =$	$\delta_c = \frac{\dots\dots\dots}{EI}$

DR. Ahmed M. EL-Kholy